

X product.

$$\mathbf{V} := \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix} \quad \mathbf{Q} := \begin{bmatrix} q_1 \\ q_2 \\ q_3 \end{bmatrix} \quad \mathbf{V} = \begin{pmatrix} 0 \\ 2 \\ 0 \end{pmatrix} \quad \mathbf{Q} = \begin{pmatrix} 2 \\ 0 \\ 0 \end{pmatrix} \quad \mathbf{V} \times \mathbf{Q} = \begin{pmatrix} 0 \\ 0 \\ -4 \end{pmatrix}$$

$\theta$  the angle between the vectors is:  $\theta := \frac{\pi}{2}$

$$\mathbf{V} \times \mathbf{Q} = \begin{matrix} v_2 \cdot q_3 - v_3 \cdot q_2 = 0 \\ v_3 \cdot q_1 - v_1 \cdot q_3 = 0 \\ v_1 \cdot q_2 - v_2 \cdot q_1 = -4 \end{matrix} = \mathbf{V} \times \mathbf{Q} = \begin{pmatrix} 0 \\ 0 \\ -4 \end{pmatrix} \quad \text{and is orthogonal to V and Q}$$

$$\mathbf{V\_length} := \sqrt{(v_1)^2 + (v_2)^2 + (v_3)^2} \quad \mathbf{Q\_length} := \sqrt{(q_1)^2 + (q_2)^2 + (q_3)^2}$$

$$\mathbf{V\_length} = 2$$

$$\mathbf{Q\_length} = 2$$

$$\mathbf{V\_length} \cdot \mathbf{Q\_length} \cdot \sin(\theta) = 4 \quad = \quad |\mathbf{V}| \cdot |\mathbf{Q}| \cdot \sin(\theta) = 4 \quad = \quad |\mathbf{V} \times \mathbf{Q}| = 4$$

Observe: if  $\mathbf{V} \parallel \mathbf{Q}$  then  $|\mathbf{V} \times \mathbf{Q}| = 0$

$$\text{Test:} \quad \theta := \text{asin}\left(\frac{4}{|\mathbf{V}| \cdot |\mathbf{Q}|}\right) \quad \text{so..} \quad 2 \cdot \theta = 3.142 \quad \text{see} \quad \theta := \frac{\pi}{2}$$