

Integration by using partial fractions.

$$\int_2^3 \frac{x}{x^2 + 3x - 4} dx = 0.262 \implies \text{that we will split the function in fractions before we solve the integral.}$$

$$\text{if } \frac{x}{x^2 + 3x - 4} = \frac{A \cdot (x + 4) + B \cdot (x - 1)}{(x + 4) \cdot (x - 1) \cdot K} \implies A := 1 \quad B := 4 \quad K := 5 \quad \text{so..}$$

$$\frac{x}{x^2 + 3x - 4} = \frac{1}{K} \cdot \left(\frac{A}{x - 1} + \frac{B}{x + 4} \right)$$

$$\text{Test: if } x=6 \text{ then } \frac{1}{5} \cdot \left(\frac{1}{x - 1} + \frac{4}{x + 4} \right) = 0.12 \quad \text{as is } \frac{x}{x^2 + 3x - 4} = 0.12 \quad \text{so...}$$

$$\text{if } f(x) := \frac{1}{x - 1} \quad \text{then} \quad F(x) := \ln(x - 1)$$

$$\frac{1}{K} \cdot \int_2^3 \left(\frac{A}{(x - 1)} + \frac{B}{(x + 4)} \right) dx = \frac{1}{K} \cdot (A \cdot \ln(3 - 1) - A \cdot \ln(2 - 1) + B \cdot \ln(3 + 4) - B \cdot \ln(2 + 4)) = 0.262$$